

# High-Capacity Reversible q-ry Data Hiding with Location Map-Free Capability.

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# Outline

- Proposed scheme
  - introduction to data hiding
  - common DE scheme:
    - *Tian's DE embedding , flowchart, prediction operation*
  - proposed data embedding algorithm
  - data extraction and image recovery
- Experimental results
- Conclusions
- Referencias

# Introduction to data hiding

## **Data hiding:**

- reversible (lossless) vs. non-reversible (lossy);
- spatial vs. transform domain;
- histogram shifting vs. difference expansion (DE) embedding.

## **Requirements:**

- Imperceptibility;
- Robustness;
- Capacity.

# DE data embedding (Tian)

- Reversibly embed a bit in difference number

$$h' = 2h + b$$

embedded original payload

**Reversible**

**integer transform:**

$$l = \left\lfloor \frac{x+y}{2} \right\rfloor, \quad h = x - y$$

$$x = l + \left\lfloor \frac{h+1}{2} \right\rfloor, \quad y = l - \left\lfloor \frac{h}{2} \right\rfloor$$

**over/underflow control:**

$$0 \leq l + \left\lfloor \frac{h+1}{2} \right\rfloor \leq 255,$$

$$0 \leq y = l - \left\lfloor \frac{h}{2} \right\rfloor \leq 255$$



# Tian (cont.)

- $h$  is **expandable** for  $b=0,1$  if

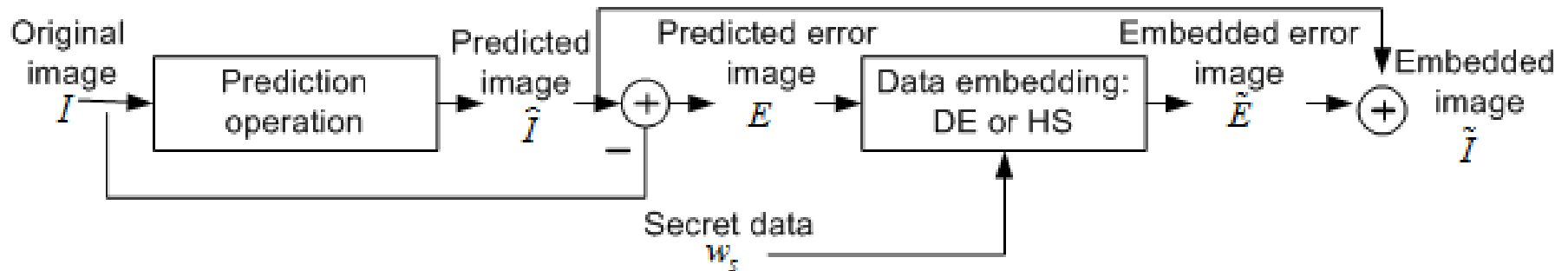
$$|h| = |2 \times h + b| = \min(2 \times (255 - l), 2 \times l + 1)$$

- Locations of expandable  $h$  are preserved in location map (LM), which is compressed by JBIG2.

## **Constraints of Tian's scheme:**

- capacity limitation;
- LM required;
- inefficient image decorrelation

# Prediction-based common DE embedding scheme



## Main constraints:

- Amount of payload;
- Amount of auxiliary data;
- Predictor-dependent.

# Prediction operation

$$E_{i,j} = I_{i,j} - \hat{I}_{i,j}$$

Original and error "Lena"



**PRE:**  $\hat{I}_{i,j} = I_{i-1,j}$

**AVG:**  $\hat{I}_{i,j} = \frac{I_{i-1,j} + I_{i,j-1}}{2}$

**MED:**

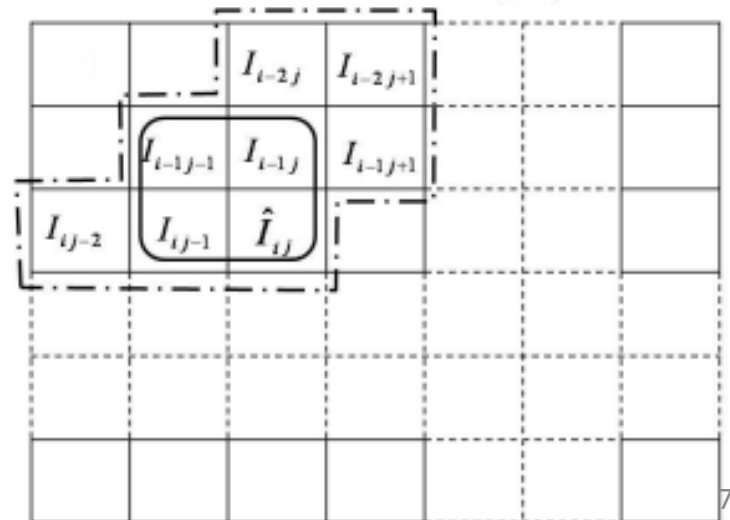
$$\hat{I}_{i,j} = \begin{cases} \min(I_{i-1,j}, I_{i,j-1}), & \text{if } I_{i-1,j-1} \leq \max(I_{i-1,j}, I_{i,j-1}) \\ \max(I_{i-1,j}, I_{i,j-1}), & \text{if } I_{i-1,j-1} \geq \min(I_{i-1,j}, I_{i,j-1}) \\ I_{i-1,j} + I_{i,j-1} - I_{i-1,j-1}, & \text{otherwise} \end{cases}$$

**GAP:**

operates on seven neighbors of the current pixel.

(a)

(b)



# The proposed **q-ryDE** scheme

## Contributions :

- **increase in payload**, using secret data with elements from Galois field  $GF(q)$ ,  $q \geq 2$  ;
- **LM free** embedding, special conditions  $T_{low}^*$ ,  $T_{high}^*$  can be found;
- Local activity indicator (**LAI**) for selection of embeddable pixels.



# Data embedding

Region used for prediction

$$\text{LAI: } d_{i,j} = \max |\Omega_{i,j} - \text{mean}(\Omega_{i,j})|$$

Two conditions to control embedding:

User-specified thresholds

$$T_{low} \leq d_{i,j} \leq T_{high}, \quad (1)$$

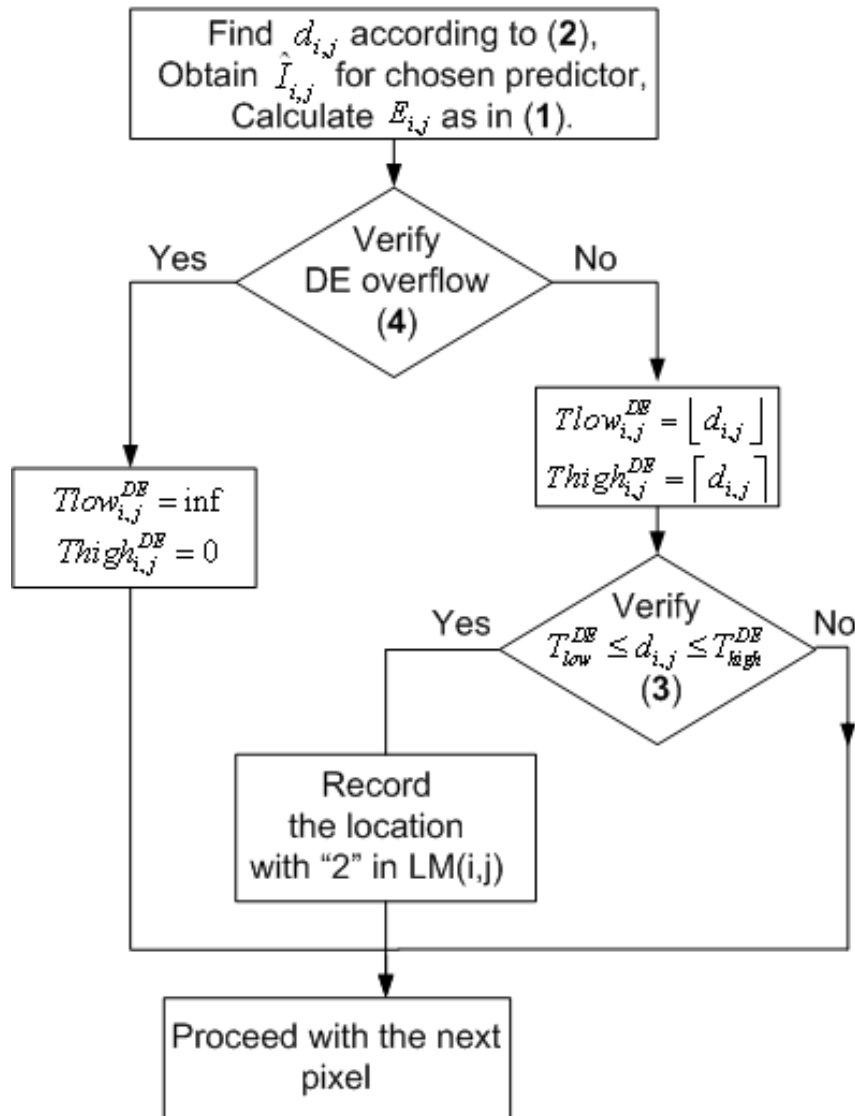
$$q \leq \hat{I}_{i,j} + q \times E_{i,j} \leq K - 1 - q, \quad (2)$$

where  $K = 2^k$  - number of image levels,  $K=256$  for 8-bit grayscale images

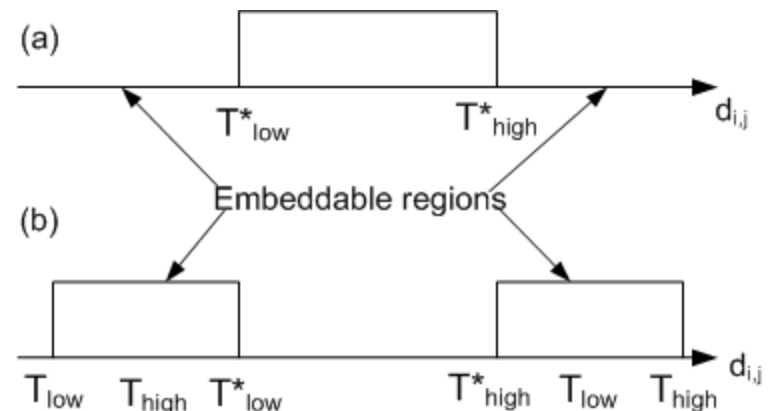
$$\tilde{I}_{i,j} = \begin{cases} \hat{I}_{i,j} + qE_{i,j} - \left\lfloor \frac{q}{2} \right\rfloor + w_s, & \text{if (1), (2) fulfilled,} \\ I_{i,j}, & \text{otherwise} \end{cases}$$

# Search of LM free conditions

## Pre-encoding stage



After we scan the image for each pixel (i,j) the thresholds for LM free embedding are obtained:

$$T_{low}^{**} = \min(T_{low}^{DE}), T_{high}^{**} = \max(T_{high}^{DE})$$


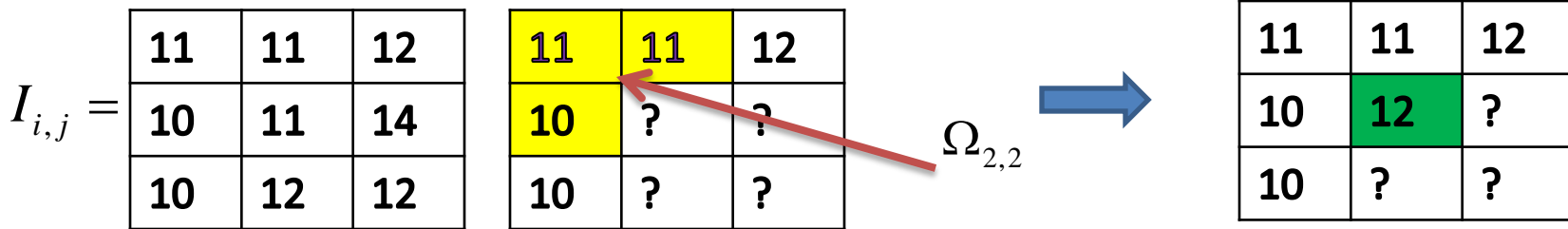
# Data extraction

Similar to embedding process:

- 1.  $E^{new}_{i,j} = \tilde{I}_{i,j} - \hat{I}_{i,j}$
- 2.  $w_s = (E^{new}_{i,j} + \lfloor \frac{q}{2} \rfloor) \bmod q,$
- 3.  $I_{i,j} = \hat{I}_{i,j} + \frac{E^{new}_{i,j} - w_s + \lfloor \frac{q}{2} \rfloor}{q}.$

# Example: data embedding

Consider, MED predictor with the region  $\Omega_{i,i}$ ,  $[T_{low}, T_{high}] = [0, 2]$ ,  $q = 2$ ,  $w_s = \{1, 0, 1, 1\}$ .



## Steps of the algorithm:

1) Prediction pixel:  $\hat{I}_{2,2} = 10$ , (check MED predictor)

2) LAI:  $d_{2,2} = \max|\Omega_{2,2} - \text{mean}(\Omega_{2,2})| = 0.67$ ,

3) Prediction error:  $E_{2,2} = I_{2,2} - \hat{I}_{2,2} = 1$ ,

4) If conditions **(1)**:  $0 \leq d_{2,2} \leq 2$ ,

and **(2)**:  $q \leq \hat{I}_{2,2} + q \times E_{2,2} \leq 255 - q$ , are correct

calculate embedded pixel  $\tilde{I}_{2,2} = \hat{I}_{2,2} + qE_{2,2} - \left\lfloor \frac{q}{2} \right\rfloor + w_s = 10 + 2 \times 1 - 1 + 1 = 12$ .

Proceed the same steps with 3 other pixels to obtain watermarked image:

$\tilde{I}_{i,j} =$

11	11	12
10	12	15
10	13	10

# Example: data extraction

Similar procedures are conducted  $\Omega_{i,i}, [T_{low}, T_{high}] = [0, 2], q = 2,$

$$\tilde{I}_{i,j} =$$

11	11	12
10	12	15
10	13	10

11	11	12
10	?	?
10	?	?

 $\Omega_{2,2}$ 


11	11	12
10	11	?
10	?	?

Proceed the same steps with 3 other pixels to obtain watermarked image:

11	11	12
10	11	14
10	12	12

 $= I_{i,j}$ 

$$w_s = \{1, 0, 1, 1\}.$$

## Steps of the recovery process:

1) Prediction pixel:  $\hat{I}_{2,2} = 10$ , (check MED predictor)

2) LAI:  $d_{2,2} = \max|\Omega_{2,2} - \text{mean}(\Omega_{2,2})| = 0.67,$

3) Prediction error:  $E_{2,2}^{new} = \tilde{I}_{2,2} - \hat{I}_{2,2} = 2,$

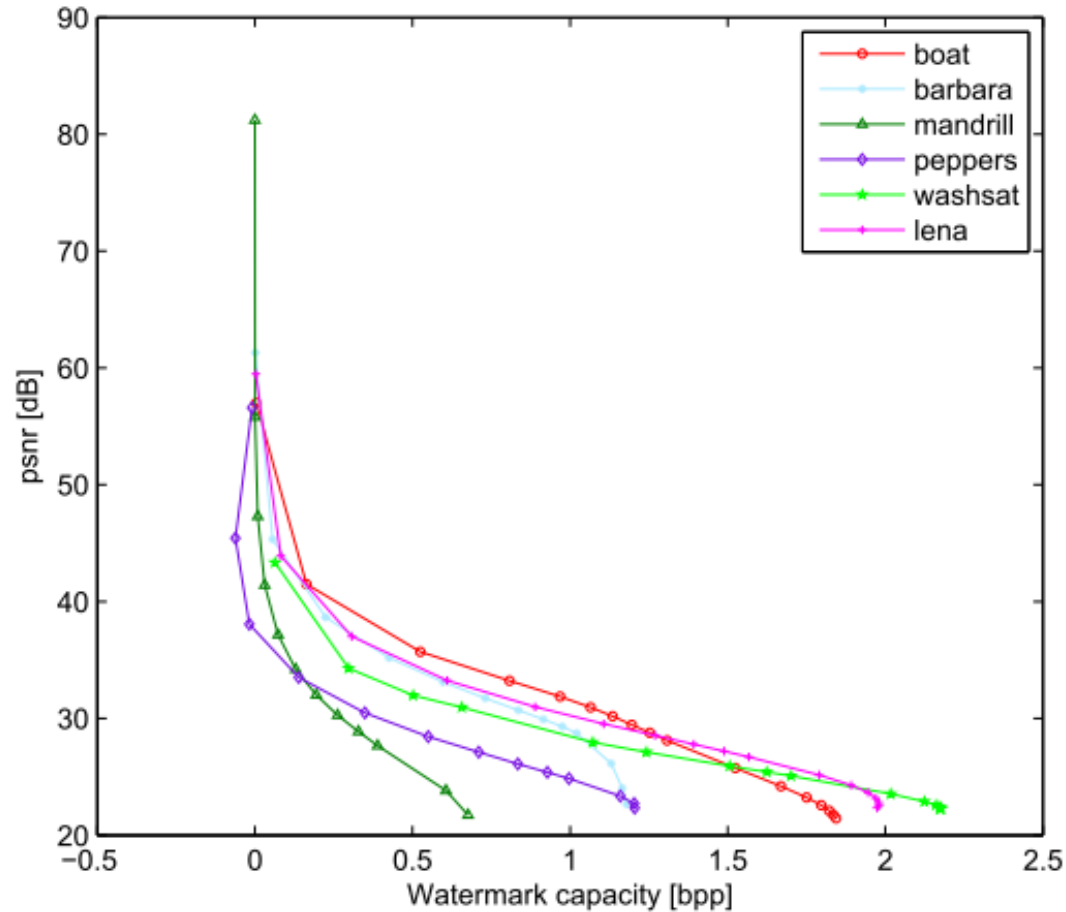
4) If conditions **(1)**:  $0 \leq d_{2,2} \leq 2$ , and **(2)**:  $q \leq \hat{I}_{2,2} + q \times E_{2,2} \leq 255 - q,$

are correct, then calculate secret data and original pixel:

$$w_s = (E_{2,2}^{new} + \left\lfloor \frac{q}{2} \right\rfloor) \bmod q = 1, \quad I_{2,2} = \hat{I}_{2,2} + \left( E_{i,j}^{new} - w_s + \left\lfloor \frac{q}{2} \right\rfloor \right) / q = 10 + (2 - 1 + 1) / 2 = 11. \quad 13$$

# Experimental results:

## 1. Increase in payload



Tian embeds 517kbits in "Lena" at 16dB while the proposed 5-ryDE scheme embeds 519kbits at 22.53dB <sup>14</sup>

## 2. LM free capability

$q$	2		3		4	
Predictor	MED	GAP	MED	GAP	MED	GAP
$T_{low}, T_{high}$	0,17	0,36	0,0	0,14	0,0	0,2
WPSNR	38.90	39.03	55.24	37.30	47.07	48.48
bpp	0.93	0.91	0.27	1.27	0.34	0.61

Table 1. The comparison of MED and GAP behavior in terms of payload and WPSNR for "House" Image.

### 3. Use of LAI

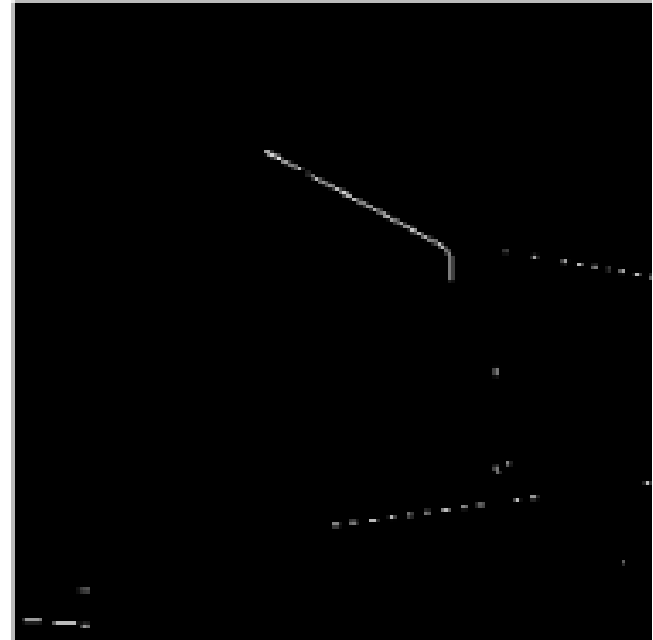
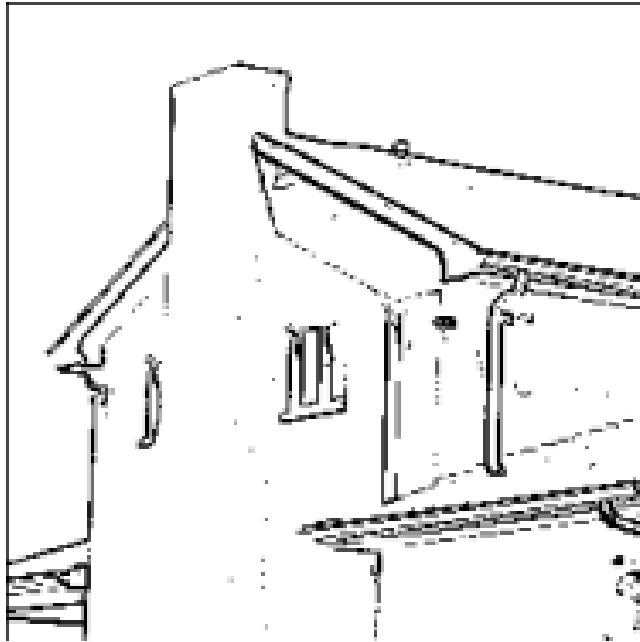
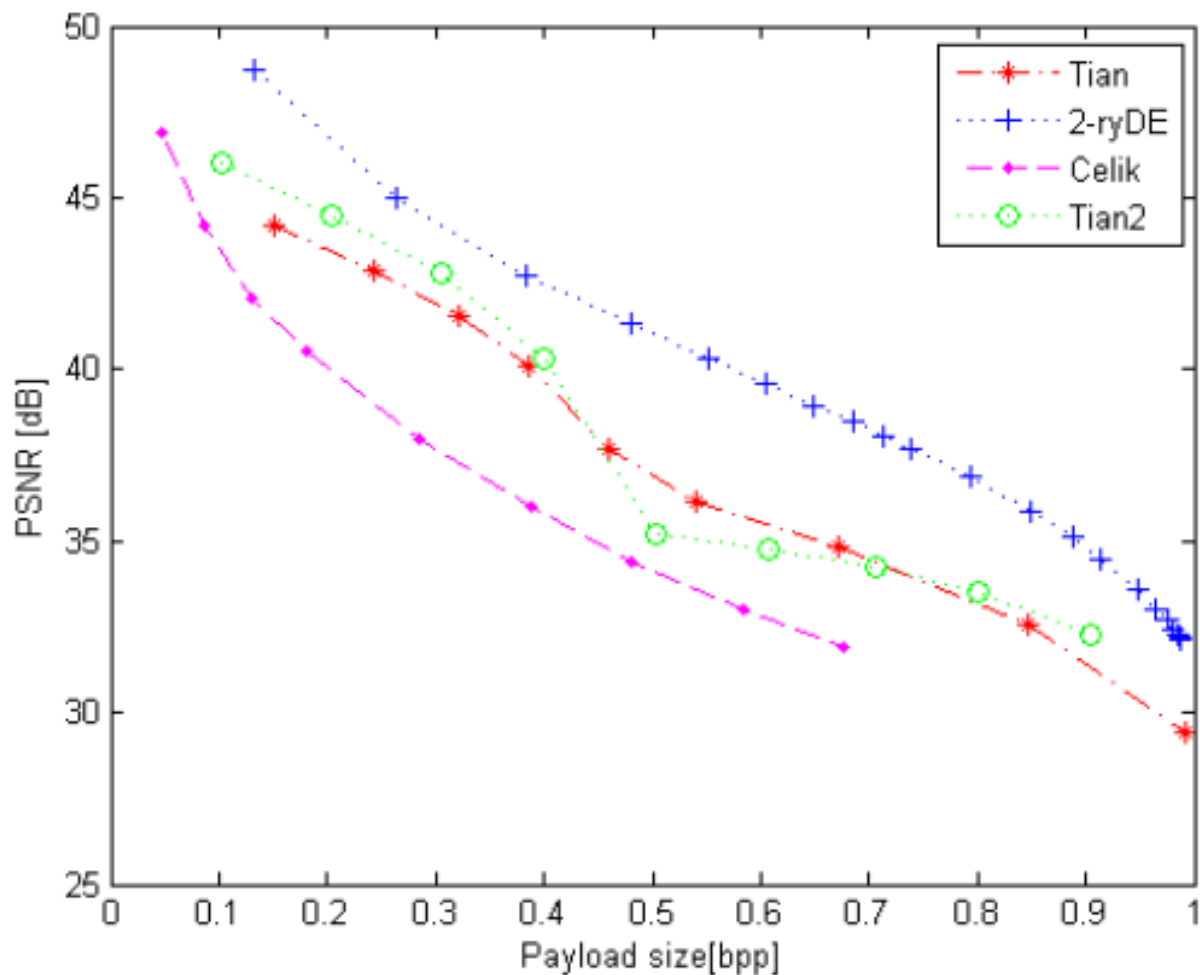


Figure Embeddable pixels positions (white color) of "House" for two pairs of thresholds ( $[0,17]$  left image and  $[59,255]$  right image corresponding to LM free embeddings).



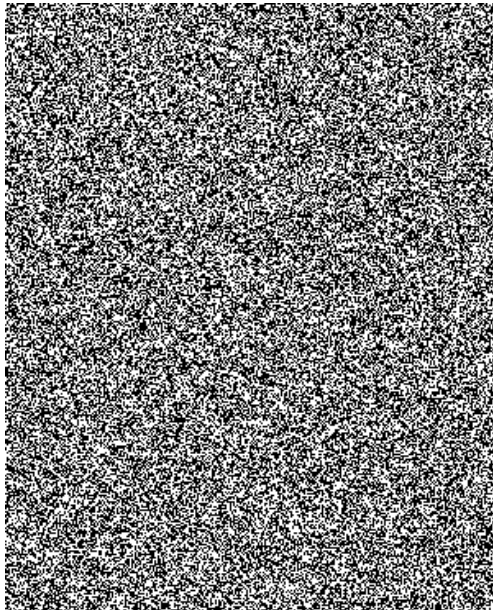
# Capacity vs. Distortion Comparison on "Lena".



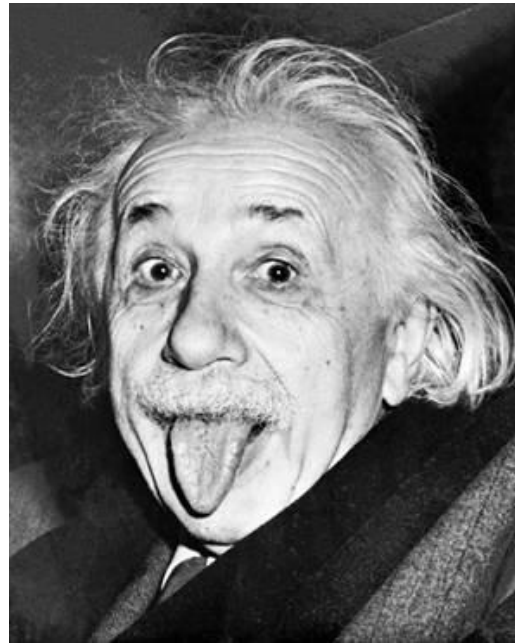
Secret message:



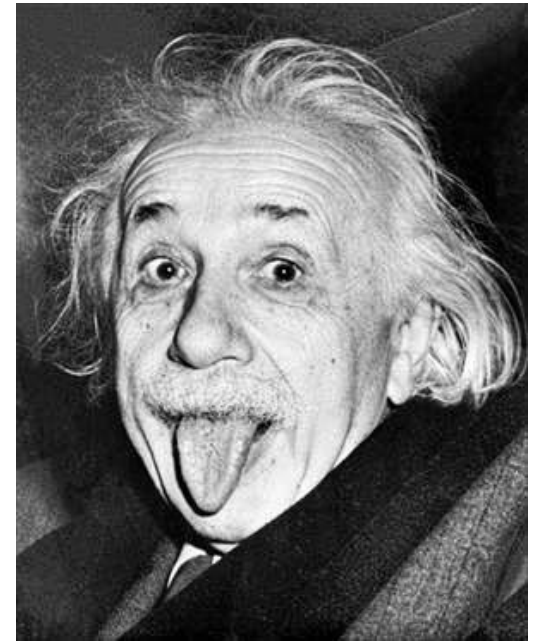
Scrambled version:



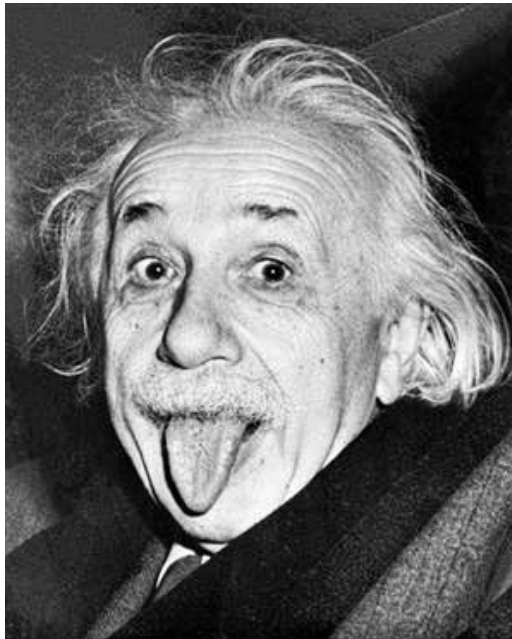
Original image:



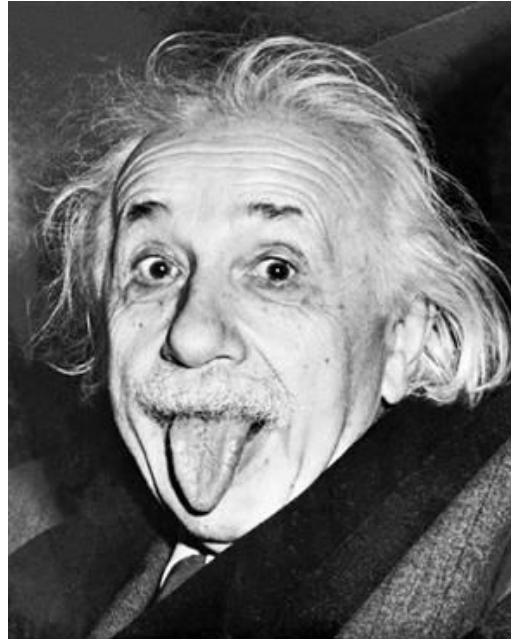
Embedded image:



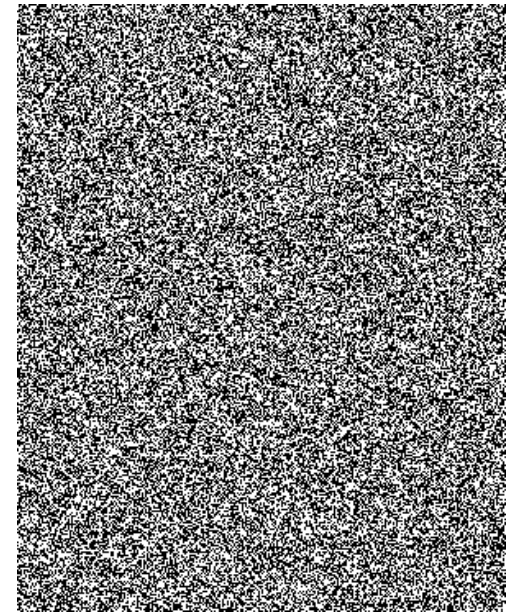
Embedded image:



Recovered original image:



Recovered scrambled data:



Recovered secret data:



# Conclusions

- an **efficient reversible DE** data-embedding method for digital images is presented;
- the performance enhancement of the proposed data hiding technique is due to the utilization of the **secret data** with the elements from **the Galois field**.
- the proved propositions enable to find the special conditions to **reduce the auxiliary data** such as the location map.
- Hence, the **payload capacity limit** and the **visual quality** are among **the best** in the literature.
- The data hiding capacity can be further increased by **multiple passes** of the corresponding scheme.

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